

Chapter 2

Spañādhikāraū - True Places of the Planets

1. The structure of the material world
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Text & Translation

2.01a adāçyarüpāu kālasya mūrtayo bhagaëāçritāu/

2.01b çghramandoccapātākhyā grahëäà gatihetavaū//

2.02a tadvātaracmibhir *baddhās tais savyetarapāëibhiū/ (2. naddhās)

2.02b prak paççād apakāñyante yathāsannaà svadii mukham//

2.03a pravahākhyo marut tāàs tu svocçābhimukham érayet/

2.03b pūrvāparākāñās te *gatià yānti pāthagvidhāu//(2. gater, pāthagvidhām)

2.04a grahāt prägbhagaëārdhasthāu präi mukhaà karñati graham/

2.04b uccasāà jī o +aparārdhasthas tadvat paççānmukhaà graham//

2.05a svocçāpakāñā *bhagaëaiū präi mukhaà yānti yad grahāu/ (2. bhagaëät)

2.05b tat teñu dhanam ity uktam äëäà paççānmukheñu *ca// (tu)

Forms of time, of invisible shape, stationed in the zodiac (bhagana), called the conjunction (sighrocca), apsis (mandocca), and node (pata), are the cause of the motion of the planets. The planets, attached to these beings by cords of air, are drawn away by them, with the right and left hand, forward or backward, according to nearness, toward their own place. A wind, moreover, called the provector (pravaha) impels them toward their own apices (ucca); being drawn away forward and backward, they proceed by a varying motion. The so called apex (ucca), when in the half orbit in front of the planet, draws the planet forward; in like manner, when in the half orbit behind the planet, it draws it backward. When the planets, drawn away by their apices (ucca), move forward in their orbits, the amount of the motion so caused

is called their excess (dhana), when they move backward, it is called their deficiency (rina).

2.06a *dakñiëottarato +apy evaà pāto *rāhuù svaraà hasā/(2. dakñiëottarator, rāhuç ca raà hasä)

2.06b vikñipaty eña vikñepaà candradénām apakramāt//

2.07a uttarābhimukhaà pāto vikñipaty aparārdhagaù/

2.07b grahaà prāgbhagaëārdhastho yāmyāyām apakarñati//

2.08a budhabhārgavayoù çēghrāt tadvat pāto *yadā sthitaù/ (2. yathāsthitaù)

2.08b tacchēghrākarñāëät tau tu vikñipyete yathoktavat//

In like manner, also, the node, Rahu, by its proper force, causes the deviation in latitude (vikshepa) of the moon and the other planets, northward and southward, from their point of declination (apakrama). When in the half orbit behind the planet, the node causes it to deviate northward; when in the half orbit in front, it drives it away southward. In the case of Mercury and Venus, however, when the node is thus situated with regard to the conjunction (sighra), these two planets are caused to deviate in latitude, in the manner stated, by the attraction exercised by the node upon the conjunction.

2.09a mahatvān maëòalasyārkaù svalpam evāpakāñyate/

2.09b maëòalālpatayā candras tato bahv apakāñyate/

2.10a bhaumādayo +alpamūrtitvāc chēghramandoccasai jī akaiù/ (2. saà jī itaiù)

2.10b daivatair apakāñyante sudūram ativegitāù//

2.11a ato dhanarēaà sumahat teñāà gativaçād bhavet/

2.11b ākāñyamāëäs tair evaà vyomni yānty anilāhatāù//

Owing to the greatness of its orb (orbit?), the Sun is drawn away only a very little: the moon, by reason of the smallness of its orb (orbit?), is drawn away much more. Mars and the rest, on account of their small size, are, by the supernatural beings (daivata) called conjunction (sighrocca) and apsis (mandocca), drawn away very far, being caused to vacillate exceedingly. Hence the excess (dhana) and deficiency (rina) of these latter is very great, according to their rate of motion. Thus do the planets, attracted by those beings, move in the firmament, carried on by the wind.

2.12a *vagrätivagrā vikalā mandā mandatarā samā/ (2. vakrānuvagrā)

2.12b tathā çēghratarā çēghrā grahāëām aññadhā gatiù//

2.13a tatrātiçēghrā çēghrākhyā mandā mandatarā samā/

2.13b ājvēti pai cadhā jī eyā *yā vagrā sātivakragā// (2. +anyā vakrādikā matā)

The motion of the planets is of eight kinds: retrograde (vakra), somewhat retrograde (anuvakra), transverse (kutila), slow (manda), very slow (mandatarā), even (samā); also, very swift (sighratarā), and swift (sighra). Of these, the very swift (atisighra), that called swift, the slow, the very slow, the even – all these five are forms of the motion called direct (riju); the somewhat retrograde is retrograde.

2.14a tattadgativaçän nityaà yathä daktulyatäà grahäu/
2.14b prayänti tat pravakñyami sphuëkaraëam ädarät//

By reason of this and that rate of motion, from day to day, the planets thus come to an accordance with their observed places (dris) – this, their correction (sphutikarana), I shall carefully explain.

2.15a räçiliptänöamo bhägaù prathamaà jyärdham ucyate/
2.15b tat tadvibhaktalabdhonamiçritaà tad dvitëyakam//

2.16a ädyenaivaà kramät piëðän bhaktvä *labdhonasaà yutäu/(2. labdhonitair yutaiù)
2.16b *khaëðakäu syuç caturviàçajyärdhapiëðäu kramäd amë//(2. khaëðakais)

2.17a tattväçvino +aì käbdhikätä rüpabhümidharartavaù/(224, 449, 691)
2.17b khäi kãñau pai caçünyeçä bæarüpaguëendavaù/(890, 1105, 1315)

2.18a çünyalocanapai caikäç chidrarüpamunëndavaù/(1520, 1719)
2.18b viyaccandrätidhätayo guëarandhräambaräçvinaù/(1910, 2093)

2.19a muniñaòyamaneträëi candrägnikâtadasrakäu/(2267, 2431)
2.19b pai cãñaviñayäkñëëi kui jaräçvinagäçvinaù/(2585, 2728)

2.20a randhrapai cãñakayamä vasvadryaì kayamäs tathä/(2859, 2978)
2.20b kätãñöaçünyajvalanä nagädriçaçivahnayaù/(3084, 3179)

2.21a ñaipai calocanaguëäç candraneträgnivahnayaù/(3256, 3321)
2.21b yamädrivahnijvalanä randhraçünyärnavägnayaù/(3372, 3401)

2.22a rüpägnisägaraguëä vasvagnikâtavahnayaù/(3431, 3438)
2.22b projjhyotkrameëa vyäsärdhäd utkramajyärdhapiëðikäu//

2.23a munayo randhrayamalä rasañäökä munëçvaräu/(7, 29, 66, 117)
2.23b dvyaññäikä rüpañäðdasräù sägarärthahutäçanäu/(182, 261, 354)

2.24a khartuvedä navädryarthä diì nägäs tryarthakui jaräu/(460, 710, 853)
2.24b nagäambaraviyaccandrä rüpabhüdharäçai karäu/(1007, 1171)

2.25a çarärëavahutäçaikä bhujai gäkñiçarendavaù/(1345, 1528)
2.25b navarüpamahédhraikä gajaikäi kaniçäkaräu//1719, 1918)

2.26a guëäçvirüpaneträëi pävakägniguëäçvinaù/(2123, 2333)
2.26b vasvarëavärthayamaläs turai gartunagäçvinaù/(2548, 2767)

2.27a navaññanavaneträëi pävakaikayamägnayaù/(2989, 3213)
2.27b gajägnisägaraguëä utkramajyärdhapiëðakäu/(3438)

The eighth part of the minutes of a sign is called the first sine (jyardha); that, increased by the remainder left after subtracting from it the quotient arising from dividing it by itself, is the second sine. Thus, dividing the tabular sines in succession

by the first, and adding them, in each case, what is left after subtracting the quotients from the first, the result is twenty-four tabular sines (jyardhapinda), in order, as follows: 225, 449, 671, 890, 1105, 1315, 1520, 1719, 1910, 2093, 2267, 2431, 2585, 2728, 2859, 2978, 3084, 3167, 3256, 3321, 3372, 3409, 3431, 3438. Subtracting these, in reverse order, from the half diameter, gives the tabular versed sines (utkramajyardhapindaka): 7, 29, 66, 117, 182, 261, 334, 460, 579, 710, 853, 1007, 1171, 1345, 1528, 1719, 1918, 2123, 2333, 2548, 2767, 2989, 3213, 3438: these are the versed sines.

2.28a paramāpakramajyā tu saptarandhraguēendavaù/(1397)

2.28b tadguēā jyā trijēvāptā taccāpaā krāntir ucyate//(2. iñyate)

The sine of the greatest declination is 1397; by this multiply any sine, and divide by the radius; the arc corresponding to the result is said to be the declination.

2.29a grahaā saā çodhya mandocçāt tathā çēghrād viçodhya ca/

2.29b çēñaā kendrapadaā tasmād bhujajyā koīr eva ca//(2. kendraā padaā)

2.30a gatād bhujajyā viñame gamyāt koīū pade bhavet/

2.30b *yugme tu gamyād bāhujyā koījyā tu gatād bhavet//(2. same)

Subtract the longitude of a planet from that of its apsis (mandocca); so also, subtract it from that of its conjunction (sighra); the remainder is its anomaly (kendra); from that is found the quadrant (pada); from this, the base sine (bhujajya), and likewise that of the perpendicular (koti). In an odd (vishama) quadrant, the base sine is taken from the part past, the perpendicular from that to come; but in an even (yugma) quadrant, the base sine (bahujya) is taken from the part to come, and the perpendicular sine from that past.

2.31a liptās tattvayamair bhaktā *labdhaā jyāpiēōikaā gatām/(2. labdhā jyāpiēōikā gatāū)

2.31b gatagamyāntarābhyastaā vibhajet tattvalocanaiù//(225)

2.32a tadavāptaphalaā yojyaā jyāpiēōe *gatasaāji ake/(2. gatasaāji ite)

2.32b syāt kramajyāvidhir ayaā utkramajyāsv api smātaù//

2.33a jyāā *projjhya çēñaā tattvāçvihataā tadvivaroddhātām/(2. projjhyānyattattvayamair hatvā)(225)

2.33b saā khyātattvāçvisaā varge *saā yojya dhanur ucyate//(2. saā yojyaā) (225)

Divide the minutes contained in any arc by two hundred and twenty five; the quotient is the number of the preceding tabular sine (jyapindaka). Multiply the remainder by the difference of the preceding and following tabular sines, and divide by two hundred and twenty five. The quotient thus obtained add to the tabular sine called the preceding; the result is the required sine. The same method is prescribed also with respect to the versed sines. Subtract from any given sine the next less tabular sine; multiply the remainder by two hundred and twenty five, and divide by the difference between the next less and next greater tabular sines; add the quotient to the product of the serial number of the next less sine into two hundred and twenty five; the result is the required arc.

2.34a raver mandaparidhyaà çä manavaù çetago radäù/ (14, 32)
3.34b yugmante viñamante tu nakhaliptonitäs tayou//

2.35a yugmante +arthädrayaù *khägnisuräù süryä navärëaväù/(2. khägniù suräs)(75, 30, 33, 12, 49)
2.35b oje dvyagä vasuyamä radä rudrä gajäbdayaù//

2.36a kujädënäà *ataù çëghrä yugmante +arthägnidasrakäù/(2. tataç çaignryä)(235)
2.36b guëägnicandräù *khanagä dvirasäkñëi go+agnayaù/(2. khägäç ca)(133, 70, 262, 39)

2.37a ojante *dvitriyamalä dviviçve yamaparvataù/(2. dvitrikayamäù)(132, 72)
2.37b khartudasrä viyadvedäù çëghrakarmaëi kértitäù/(260,40)

2.38a ojayugmántaraguëä bhujajyä trijyayoddhätä/
2.38b *yugme vätte dhanarëäà syäd ojäd ünädhike sphuäm// (2. yugmavätte)

The degrees of the Sun's epicycle of the apsis (mandaparidhi) are fourteen, of that of the Moon, thirty-two, at the end of the even quadrants; and at the end of the odd quadrants, they are twenty minutes less for both. At the end of the even quadrants, they are 75, 30, 33, 12, 49; at the odd (oja) they are 72, 28, 32, 11, for Mars and the rest. Farther, the degrees of the epicycle of the conjunction (sighra) are, at the end of the even quadrants, 235, 133, 70, 262, 39; at the end of the odd quadrants, they are stated to be 232, 132, 72, 260, 40, as made use of in the calculation of the conjunction (sighrakarman). Multiply the base sine (bhujajya) by the difference of the epicycles at the odd and even quadrants, and divide by radius (trijya); the result, applied to the even epicycle (vritta), and additive (dhana) or subtractive (rina), according as this is less or greater than the odd, gives the corrected (sphuta) epicycle.

2.39a tadguëë bhujakoõijye bhagaëäà çavibhäjite/
2.39b tadbhujajyäphaladhanur mändaà liptädikaà phalam//

By the corrected epicycle multiply the base sine (bhujajya) and perpendicular sine (kotijya) respectively, and divide by the number of degrees in a circle: then, the arc corresponding to the result from the base sine (bhujajyaphala) is the equation of the apsis (manda phala), in minutes, etc.

2.40a *çaignryäà koõiphalaà kendre makarädaù dhanaà smätam/(2. çaignre)
2.40b saàçodhyaà tu *trijëvâyäà karkyädaù koõijaà phalam/(2. trijëvätäù)

2.41a tadbähupalavargaikyän mülaà karëaç caläbhidhaù/
2.41b trijyäbhyastaà bhujaphalaà calakarëavibhäjitam//

2.42a labdhasya cäpäà liptädiphalaà *çaignryam idaà smätam/ (2. çaignram)
2.42b etad ädye kujädënäà caturthe caiva karmaëi//

The result from the perpendicular sine (kotiphala) of the distance from the conjunction is to be added to radius, when the distance (kendra) is in the half orbit beginning with Capricorn; but when in that beginning with Cancer, the result from the

perpendicular sine is to be subtracted. To the square of the sum or difference add the square of the result from the base sine (bahuphala); the square root of their sum is the hypotenuse (karna) called variable (cala). Multiply the result from the base sine by radius, and divide by the variable hypotenuse: the arc corresponding to the quotient is, in minutes, etc., the equation of the conjunction (saighrya phala); it is employed in the first and fourth process of correction (karman) for Mars and the other planets.

2.43a mändaà karmaikam arkendor bhaumädénäm athocyate/

2.43b *çaighryaà mändaà punar mändaà çaighryaà catväry anukramät//(2. çaighraà)

2.44a madhye çéghraphalasyärdhaà mädam ardhaphalaà tathä/

2.44b madhyagrahe *mandaphalaà sakalaà çaighryam eva ca//(2. punar mändaà)

2.45a ajädikendre sarveñää *çaighrye mände ca karmaëi/(2. mände çaighre)

2.45b dhanaà grahäää liptädi tulädäv reäm eva ca//

The process of correction for the apsis (manda karman) is the only one required for the Sun and Moon: for Mars and the other planets are prescribed that for the conjunction (saighrya), that for the apsis (manda), again that for the apsis, and that for the conjunction – four, in succession. To the mean place of the planet apply half of the equation of the conjunction (sighraphala), likewise half the equation of the apsis; to the mean place of the planet apply the whole equation of the apsis (mandaphala), and also that of the conjunction. In the case of all the planets, and both in the process of correction for the conjunction and in that for the apsis, the equation is additive (dhana) when the distance (kendra) is in the half orbit beginning with Aries; subtractive (rina), when in the half orbit beginning with Libra.

2.46a arkabähupaläbhyastä grahabhuktir vibhäjitä/

2.46b bhacakrakalikäbhis tu liptäü karyä grahe +arkavat//

Multiply the daily motion (bhukti) of a planet by the Sun's result from the base-sine (bahuphala), and divide by the number of minutes in a circle (bhacakra); the result, in minutes, apply to the planet's true place, in the same direction as the equation was applied to the Sun.

2.47a svamandabhuktisaà çuddhä madhyabhuktir niçäpateü/

2.47b dorjyantarädikaà kätvä bhuktäv äädhanaà bhavet//

2.48a grahabhukteü phalaà käryaà grahavan mandakarmaëi/

2.48b dorjyantaraguëä bhuktis tattvanetroddhätä punaü// (225)

2.49a svamandaparidhikñuëëä bhagaëää çoddhätä kaläü/

2.49b karkyadau tu dhanaà tatra makarädäv äëää smätam//

From the mean daily motion of the Moon subtract the daily motion of its apsis (manda), and, having treated the difference in the manner prescribed by the next rule, apply the result, as an additive or subtractive equation, to the daily motion. **The equation of the planet's daily motion is to be calculated like the place of the planet in the process for the apsis: multiply the daily motion by the difference of tabular sines**

corresponding to the base-sine (dorjya) of anomaly, and then divide by two hundred and twenty five; Multiply the result by the corresponding epicycle of the apsis (mandaparidhi), and divide by the number of degrees in a circle (bhagana): the result, in minutes, is additive when in the half-orbit beginning with Cancer, and subtractive when in that beginning with Capricorn.

2.50a mandasphuökâtâà bhuktià projjhya çéghroccabhuktitaù/

2.50b taccheçaà vivareëätha hanyät trijyântyakarëayoù//

2.51a calakarëähâtaà bhuktau karëe trijyâdhike dhanam/

2.51b äëam üne +adhike projjhya çëñaà vakragatir bhavet//

Subtract the daily motion of a planet, thus corrected for the apsis (manda), from the daily motion of its conjunction (sighra); then multiply the remainder by the difference between the last hypotenuse and radius, and divide by the variable hypotenuse (cala karna): the result is additive to the daily motion when the hypotenuse is greater than the radius, and subtractive when this is less: if, when subtractive, the equation is greater than the daily motion, deduct the latter from it, and the remainder is the daily motion in a retrograde (vakra) direction.

2.52a dÛrasthitaù svaçéghroccäd grahaù çithilaraçmibhiù/

2.52b savyetaräkântatanur bhavet vakragatis tadâ//

2.53a kâtartucandrair vedendraiù çünyatryekair guëãñöabhiù/(164, 144, 130, 83?)

2.53b çararudraiç caturtheñu kendràà çair bhÛsutädayaù//((115)

2.54a bhavanti vakriëas tais tu svaiù svaiç cakräd viçodhitaiù/

2.54b avaçiñöäà çatulyaiù svaiù kendrair ujjhanti vakratäm//

2.55a mahattvac chéghraparidheù saptame bhâgubhÛsutau/

2.55b añöame jëvaçaçaijau navame tu çanaiçcaraù//

When at a great distance from its conjunction (sighrocca), a planet, having its substance drawn to the left and right by slack cords, comes then to have a retrograde motion. Mars and the rest, when their degrees of commutation (kendra), in the fourth process, are, respectively, 164, 144, 130, 163(?) and 115, become retrograde (vakrin): and when their respective commutations are equal to the number of degrees remaining after subtracting those numbers, in each several case, from a whole circle, they cease retrogradation. In accordance with the greatness of their epicycles of the conjunction (sighraparidhi), Venus and Mars cease retrograding in the seventh sign, Jupiter and Mercury in the eighth, Saturn in the ninth.

2.56a kujärkigurupätänäà grahvac chéghrajaà phalam/

2.56b vämaà tätëyakaà mändaà budhabhãrgavayoù phalam//

2.57a svapätönäd grahãj jëvã çéghräd bhâgujasaumyayoù/

2.57b vikñepaghny antyakarëäptã vikñepas trijyayã vidhoù//

2.58a vikñepãpakramaikatve krântir vikñepasaà yutã/

2.58b digbhede viyutã spañöã bhãskarasya yathãgatã//

To the nodes of Mars, Saturn, and Jupiter, the equation of the conjunction is to be applied, as to the planets themselves respectively; to those of Mercury and Venus, the equation of the apsis, as found by the third process, in the contrary direction. The sine of the arc found by subtracting the place of the node from that of the planet – or, in the case of Venus and Mercury, from that of the conjunction – being multiplied by the extreme latitude, and divided by the last hypotenuse – or, in the case of the Moon, by Radius – gives the latitude (vikshepa). When the latitude and declination (apakrama) are of like direction, the declination (kranti) is increased by the latitude; when of different direction, it is diminished by it, to find the true (spashta) declination: that of the Sun remains as already determined.

2.59a grahodayapräehatä khakhāññaikoddhātā gatiù/
2.59b cakrāsavo labdhayutā svāhorātrāsavaù smātāù//

Multiply the daily motion of a planet by the time of rising of the sign in which it is, and divide by eighteen hundred; the quotient add to, or subtract from, the number of respirations in a revolution: the result is the number of respirations in the day and night of that planet.

2.60a krānteù kramotkrammajye dve kâtvā tatrotkramajyayā/
2.60b hēnā trijyā dinavyāsadalaà taddakñiēottaram//

Calculate the sine and versed sine of declination: then radius, diminished by the versed sine, is the day-radius: it is either south, or north.

2.61a krāntijyā viñuvadbhāghné kñitijyā dvādaçoddhātā/
2.61b trijyāguēāhorātrārdhakarēptā carajāsavaù//

2.62a tatkārmukam udakkrāntau *dhanāçané pāthaksthite/(2. dhanahānē)
2.62b svāhorātracaturbhāge dinarātridale smāte//

2.63a yāmyakrāntau viparyaste dviguēe tu dinakñape/
2.63b vikñepayuktonitayā krāntyā bhānām api svake//

Multiply the sine of declination by the equinoctial shadow, and divide by twelve; the result is the Earth-sine (kshhitjya); this, multiplied by radius and divided by the day-radius, gives the sine of ascensional difference (cara): the number of respirations due to the ascensional difference is shown by the corresponding arc. Add these to, and subtract them from, the fourth part of the corresponding day and night, and the sum and remainder are, when declination is north, the half-day and half-night; when declination is south, the reverse; these, multiplied by two, are the day and night. The day and the night of the asterisms (bha) may be found in like manner, by means of their declination, increased or decreased by their latitude.

2.64a bhabhogo +aññaçatēliptāù khāçviçailās tathā titheù/
2.64b grahaliptābhabhogāptā bhāni bhuktyā dinādikam//

The portion (bhoga) of an asterism (bha) is 800 minutes; of a lunar day (tithi), in like manner, 720. If the longitude of a planet, in minutes, be divided by the portion of an

asterism, the result is its position in asterisms: by means of the daily motion are found the days, etc.

2.65a ravēnduyogalīptābhyo yogā bhabhogabhājītāù/
2.65b gatā gamyāç ca ñāñōighnyo bhuktīyogāptanāōikāù//

From the number of minutes in the sum of the longitudes of the Sun and Moon are found the yogas, by dividing that sum by the portion (bhoga) of an asterism. Multiply the minutes past and to come for the current yoga by sixty, and divide by the sum of the daily motion of the two planets: the result is the time in nadis.

2.66a arkonacandralīptābhyas tithayo bhogabhājītāù/
2.66b gatā gamyāç ca ñāñōighnyo nāōyo bhuktyantaroddhātāù//

From the number of minutes in the longitude of the Moon diminished by that of the Sun are found the lunar days (tithis), by dividing the difference by the portion (bhoga) of a lunar day. Multiply the minutes past and to come of the current lunar day by sixty, and divide by the difference of the daily motion of the two planets: the result is their time in nadis.

2.67a dhruvāēi çakunir nāgaà tātēyaà tu catuñpadam/
2.67b kià stughnaà tu caturdaçyāù kâñēyāç çāparārdhataù//

2.68a bavādēni tataù sapta carākhyakaraēāni ca/
2.68b māse +añōākātva ekaikaà karaēānāà pravartate//

2.69a tithyardhabhogaà sarveñāà karaēānāà prakalpayet/
2.69b eñā sphutagatiù proktā sūryādēnāà khacāriēām//

The fixed (dhruva) karanas, namely Sakuni, Naga, catuspada the third, and Kinstughna, are counted from the latter half of the fourteenth day of the dark half-month. After these, the karanas are called moveable (cara), namely Bava, etc., seven of them: each of these karanas occurs eight times in a month. Half the portion (bhoga) of a lunar day is established as that of the karanas. Thus has been declared the corrected (sphuta) motion of the Sun and the other planets.